

Fig. 1. Effect of noise hole.

Introduction

Character thinning is used as a preprocessing stage in OCR to simplify the subsequent recognition problem. However, specific defects in the data can cause thinning algorithms to destroy information and lead to misrecognition. The number and importance of such defects are particular to each problem and its application, and their effect on a thinning algorithm can only be estimated by experiment. Three such common data defects are 1) the presence of several sorts of small holes which lead to spurious loops in the skeleton, 2) single element edge irregularities which lead to spurious tails, and 3) acute angles between limbs which lead to distortions and results also having spurious tails.

Most thinning algorithms discussed in the literature [1]–[8] rely on the steady erosion of character boundaries while maintaining the connectivity of the shape. All are sensitive to one or more of the above data defects. Connectivity rules tend to overemphasize the importance of small holes and produce topologically incorrect skeletons with spurious loops (Fig. 1). Tenuously connected irregularities residing on limb edges (Fig. 2) gain exaggerated importance by being labeled as "limb ends" very early in the thinning process. This leads to the generation of spurious tails.

It is a characteristic of boundary eroding algorithms that more material is removed from one side of a character limb than the other if the perimeter is longer. This means that limbs will tend to be eroded much more rapidly from the outside of an acute angle junction than from the inside. This leads to the production of an extra tail (Fig. 3) or to a "necking" effect at cross overs (Fig. 4).

In this correspondence the problems are considerably reduced by the introduction of some preprocessing stages before a standard thinning algorithm is applied. These preprocessing heuristics are specifically aimed at reducing the failure rate due to the above defects in the data.

PREPROCESSING

A. Hole Removal

In this work characters are restricted to black and white elements arranged in a 16×24 matrix. Preprocessing begins with the detection of six types of hole by raster scanning the character with six patterns of bits. Three of these (H_i) will fit all holes containing one or two elements (Fig. 5) and the remaining three (I_i) will fit the same size of hole (Fig. 6) but only if the hole is embedded at least two elements deep in a limb.

Embedded holes identified by the I_i are likely to represent a real loop in the character and are retained. Other holes identified

Some New Heuristics for Thinning Binary Handprinted Characters for OCR

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Abstract—A standard thinning algorithm which consists of a matrix matching scheme [1] used in conjunction with a connectivity measure [2] is briefly described. Several new heuristics are introduced to obviate some of the common shortcomings of thinning algorithms when applied to handprinted data.

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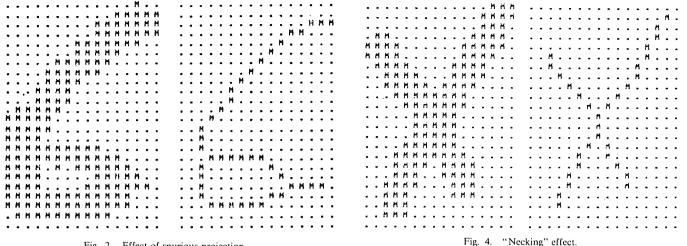


Fig. 2. Effect of spurious projection.

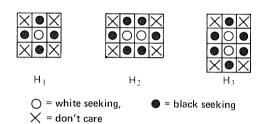


Fig. 5. Hole detectors.

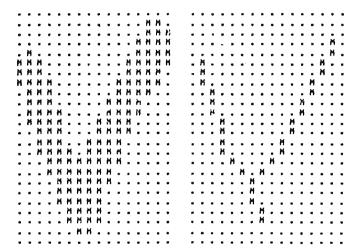


Fig. 3. Tail generation at acute limb angle.

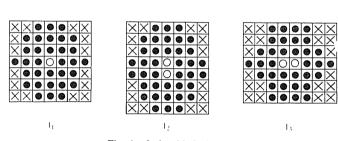


Fig. 6. Isolated hole detectors.

by the H_i are located fairly close to a limb edge and can be attributed to the effects of noise. These holes are removed by 1) merging the hole with adjacent white areas by the removal of black elements, or 2) filling it with additional black elements.

B. Smoothing

The second preprocessing stage is the removal of all black elements having less than three black neighbors and having connectivity 1 (Appendix). This has the effect of removing single element projections and all isolated spots having one or two elements.

C. Acute Angle Emphasis

The final preprocessing stage involves the detection of upward and downward acute angles between limbs by again scanning the character with patterns of bits. Five of these (D_i) will fit the sharpest forms of downward pointing acute angles (Fig. 7) and a reflected set (U_i) will fit upward pointing acute angles. After a fit is found the central black element is deleted and the process is repeated twice more. The second and third iterations are only carried out if the preceding iteration effected a deletion. Only D_i , U_i , i = 1, 2, 3 are scanned during the second iteration and only D_1 , U_1 on the third, since fits are not possible with the other patterns. This heuristic compensates for much of the uneven thinning by increasing the length of the boundary on the inside of

angled intersections. The result of such preprocessing on the character shown in Fig. 3 is shown in Fig. 8.

D. Summary

The preprocessing algorithms described in this section can be described more formally as follows:

- Identify character hole which matches an H_i .
- Given a match in Step 1, if one of the picture elements at the top left, top right, bottom right, or bottom left corner of H_i is white then take first such and mark its two black neighbors for deletion; else if none of I_m m = 1, 2, 3 fits the hole then mark hole for filling.
- Step 3 Return to Step 1 until all such holes have been identified.
- Step 4 Delete all marked elements.
- Step 5 Fill all marked holes.
- Step 6 Remove elements having two, one, or no black neighbors and having connectivity 1 or 0.
- Step 7 Identify upward or downward acute angle fitting U_i or $D_i (i = 1, 2, \dots, 5).$
- Step 8 For each fit the central element is marked for deletion.
- Loop to Step 7 until all such fits have been detected. Step 9
- Step 10 Delete all marked elements.
- Step 11 If elements have been deleted in Step 10 repeat Steps 7–10 but using only U_i , D_i (i = 1, 2, 3); otherwise Exit.

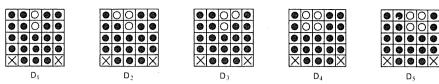


Fig. 7. Downward angle detectors.

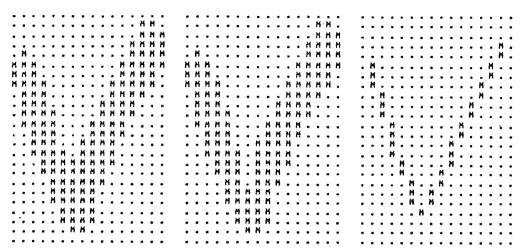


Fig. 8. Application of acute angle emphasis heuristic.

Step 12 If elements have been deleted in Step 11 repeat Steps 7-10 using U_1 and D_1 only.

Step 13 Exit.

THINNING ALGORITHM

After preprocessing, a variation of a standard thinning algorithm (1) is applied. Four matrices (M_i) in Fig. 9 are scanned over the character, and wherever a matrix fits the central black element is marked for deletion. Elements are not so marked if they are limb endpoints or if the connectivity measure for that point (Appendix) is greater than one. An endpoint is defined as a black element which is 8-connected to only one other black element. Elements already marked are considered to be white for the purpose of subsequent end point or connectivity calculations. When all four matrices have been scanned in this way, all marked elements are deleted and the process repeated until no more erosion can take place.

The results of such a thinning process are sensitive both to the order of application of the M_i and also the direction of scan. An ordering which minimizes spurious tail production is given in Table I. For example M_3 , the south edge eroding matrix, is scanned from right to left moving upwards across the character.

This algorithm can be summarized as follows.

- Step 1 Scan matrix M_1 across character according to Table I and identify next fit position.
- Step 2 If the central element at a fit is not an endpoint and has connectivity value one, then mark it for deletion.
- Step 3 Repeat Steps 1 and 2 for all fit positions.
- Step 4 Repeat Steps 1-3 for each of M_2 , M_3 , M_4 .
- Step 5 Delete all marked elements.
- Step 6 If one or more elements are deleted in Step 4 then return to Step 1.
- Step 7 Exit.

RESULTS AND DISCUSSION

Results on an unseen test set of 680 unconstrained handprinted alphanumeric characters indicated that less than 1 percent of thinning failures could be attributed to the algorithm. A signifi-









Fig. 9. Thinning matrices.

TABLE I MATRIX ORDERING AND SCAN DIRECTIONS

ORDER OF APPLICATION	DIRECTION OF SINGLE SCAN LINE	DIRECTION OF SUCCESSIVE SCAN LINES
М ₁	Left to Right	Downwards
и ₂	Upwards	Left to Right
м ₃	Right to Left	Upwards
м ₄	Downwards	Right to Left

cant reduction in confusions between the class pairs (K, X), (H, X), (V, Y), and (H, M) were recorded after thinning using the preprocessing heuristics.

Improvements beyond the 1 percent failure rate would follow the identification of more complex configurations of character elements which lead to the remaining commonest types of thinning failures.

Hardware and processing requirements go up as the size and number of matching matrices are increased. However the basic binary matching process is common to the thinning, the hole detection, and the acute angle detection. This means that existing image processing hardware designs working at video rates [9] are able to carry out the required tasks quite economically. Smoothing, end point detection, and the calculation of connectivity values are carried out rapidly using a "table-lookup" scheme for all possible 3 × 3 configurations.

APPENDIX

The connectivity measure N used is one defined by Yokoi et al. [2] as follows:

$$N(\gamma_0) = \sum_{K \in S} (\bar{\gamma}_K - \bar{\gamma}_K \cdot \bar{\gamma}_{K+1} \cdot \bar{\gamma}_{K+2})$$

where

$$S = \{1, 3, 5, 7\}$$

$$\overline{\gamma}_K = 1 - \gamma_K$$

$$\gamma_j = \gamma_{j-8} \quad \text{for } j > 8$$

and the eight neighboring pixels of γ_0 are labeled:

$$\gamma_4 \gamma_3 \gamma_2$$
 $\gamma_5 \gamma_0 \gamma_1$ with $\gamma_i = 0$ if white
 $\gamma_6 \gamma_7 \gamma_8$ = 1 if black

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